

# **Scalable MLFMA Code for Single And Multiple Targets over a Half Space**

**CHSSI CEA-9**

**Lawrence Carin, <sup>1</sup>Anders Sullivan, John Board, John Pormann,  
Eric Jones, James Pickelsimer, Paul Pauca, Zhijun Liu**

**Department of Electrical & Computer Engineering  
Duke University  
Durham, NC 27708-0291  
lcarin@ee.duke.edu**

**<sup>1</sup>Army Research Laboratory  
Radar Branch  
Adelphi, MD**

# CEA-9: Electromagnetic Sensing of Surface and Subsurface Targets: Simulation and Signal Processing

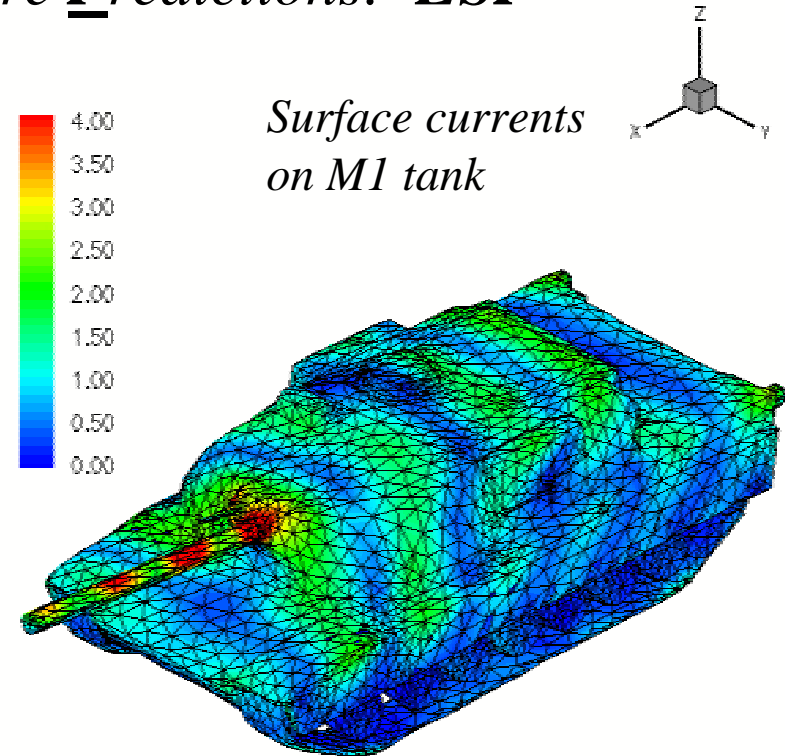
## “Electromagnetic Signature Predictions: *ESP*”

### ■ Synopsis

- **Objective:** Develop scalable MoM and MLFMA software for simulating radar scattering from targets in/above soil (mines, UXO, vehicles, bunkers, trees, etc.). Use results of EM models to train physics-based signal processing algorithms (e.g. Hidden Markov Model)
- **Partners:** Duke University and ARL
- **Development Paradigm:** FORTRAN 90; C; MPI; X-windows GUI , Python

### ■ Performance Goals

- Alpha Review completed 19 Oct 2001
- Beta Review scheduled 4QFY02
- **Operating Platforms:** IBM SP-P3, SGI O2k, Linux clusters
- **Scalability goal:** 50% speedup on 128 processors
- **Threshold:** 40% speedup on 64 processors



### ■ Management

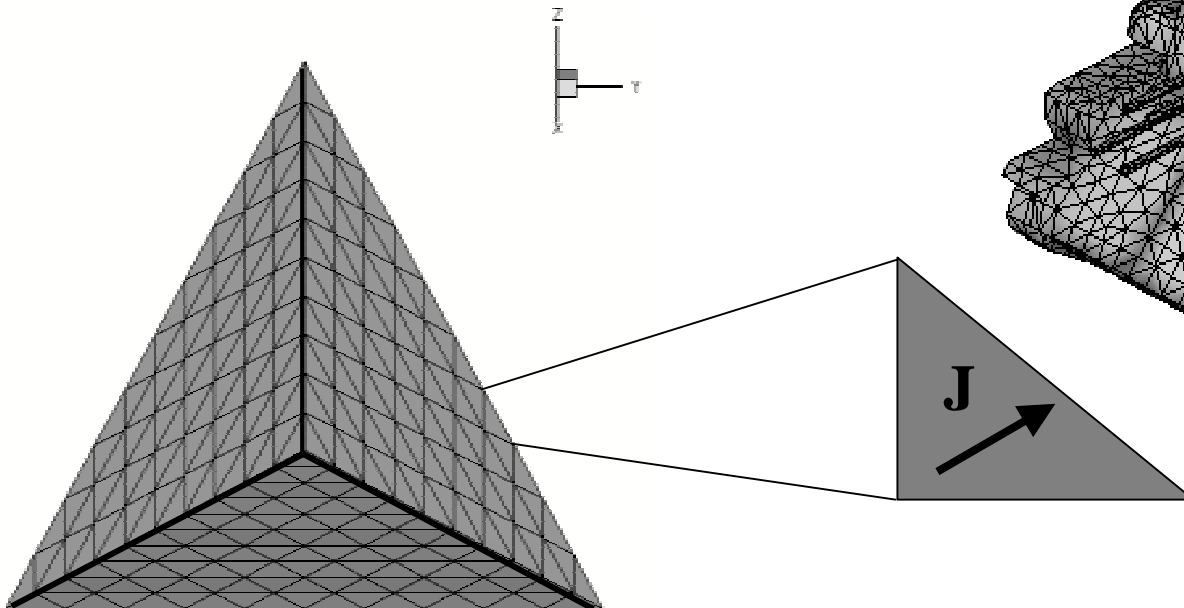
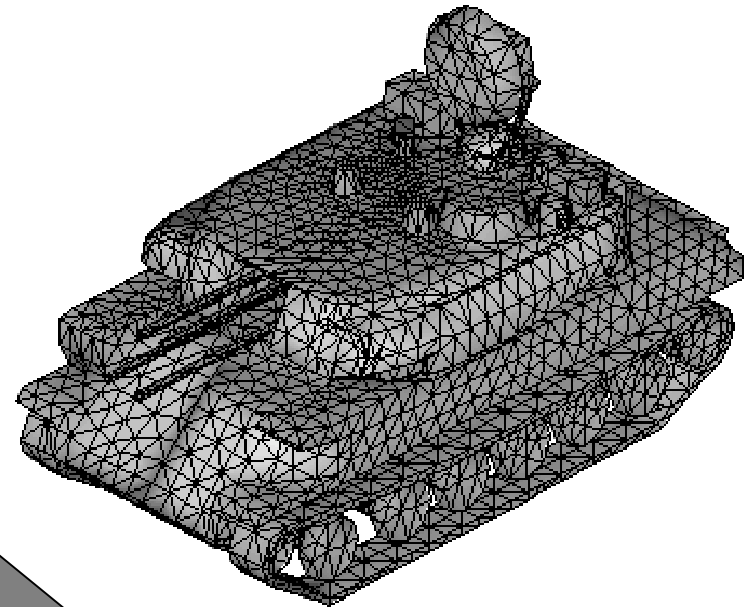
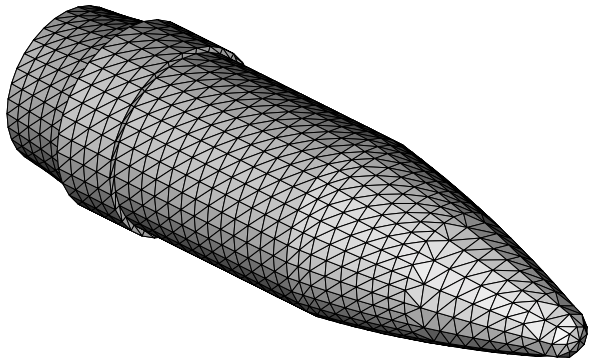
- **CHSSI:** \$500k/year – for 3 years
- **Leveraging:** \$500k/yr (ARO & SERDP), \$6M demining MURI (5 yrs)
- **Transition Approach:** Serial MoM and MLFMA codes routinely employed by ARL & NVESD

# Outline

- Brief review of Method of Moments (MoM) and Multi-Level Fast-Multipole Algorithm (MLFMA) for single target above a lossy half space (soil); scalable formulation
- Extension to an arbitrary number of targets in the presence of a half space
  - Target under trees
  - Propagation through foliated terrain
- Summary

# MLFMA/MoM – Review

*As in all such problems, numerical challenge is calculation of the electric surface currents ( $\mathbf{J}$ ) on the target surface*



# Governing Equations

- Boundary condition for perfect conductor:

$$\mathbf{E}_{\text{tan}} = 0$$

- Total field expressed as:

$$\mathbf{E}_{\text{tan}} = [ \mathbf{E}^{\text{inc}} + \mathbf{E}^{\text{s}} ]_{\text{tan}} \Rightarrow -\mathbf{E}^{\text{s}} = \mathbf{E}^{\text{inc}}$$

- Using the equivalence principle:

$$j\omega\mu \iint_S \mathbf{K}^{\tau} \cdot \mathbf{J} ds' + \frac{j}{\epsilon\omega} \nabla \iint_S \mathbf{K}_e \nabla' \cdot \mathbf{J} ds' = \mathbf{E}_{\text{tan}}^{\text{inc}}$$


$$[\mathbf{Z}][\mathbf{J}] = [\mathbf{E}^{\text{inc}}]$$

# Review of the Method of Moments (cont.)

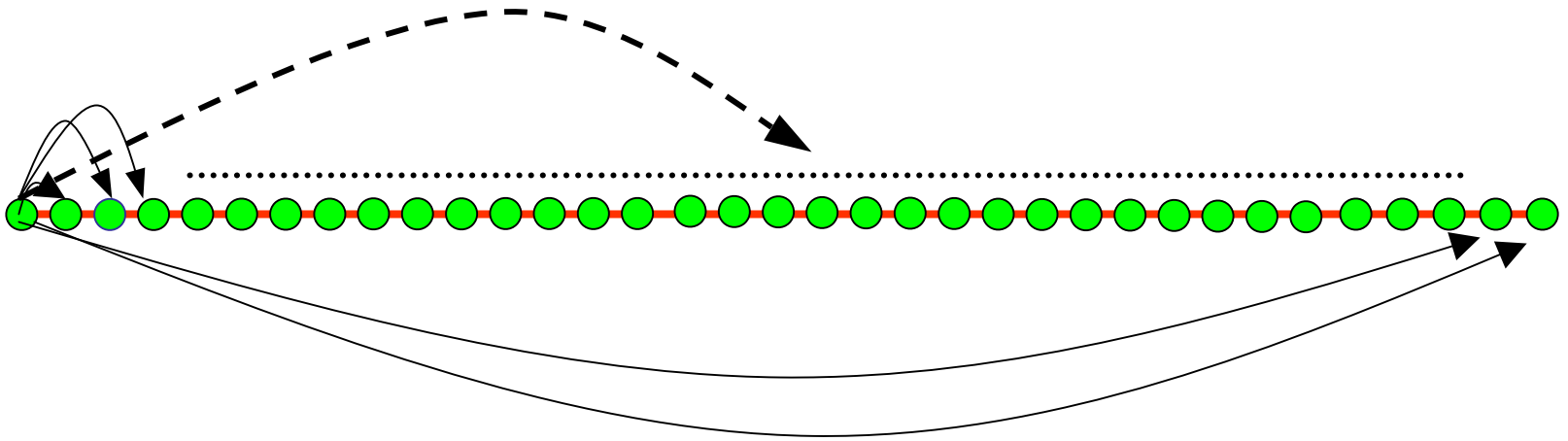
Solving:  $[\mathbf{Z}][\mathbf{J}] = [\mathbf{E}^{\text{inc}}]$

1. Direct solver using LU decomposition :  $O(N^3)$
2. Iterative solver (CG) for the linear equations:  $O(P \cdot N^2)$
3. Store impedance matrix needs RAM:  $O(N^2)$

*Our VHF T-72 tank model has  
12087 unknowns  $\Rightarrow$  2.2 GBytes RAM*

# Looking at Impedance Matrix: $\mathbf{Z}$

MoM: individual interaction between basis function and testing function.

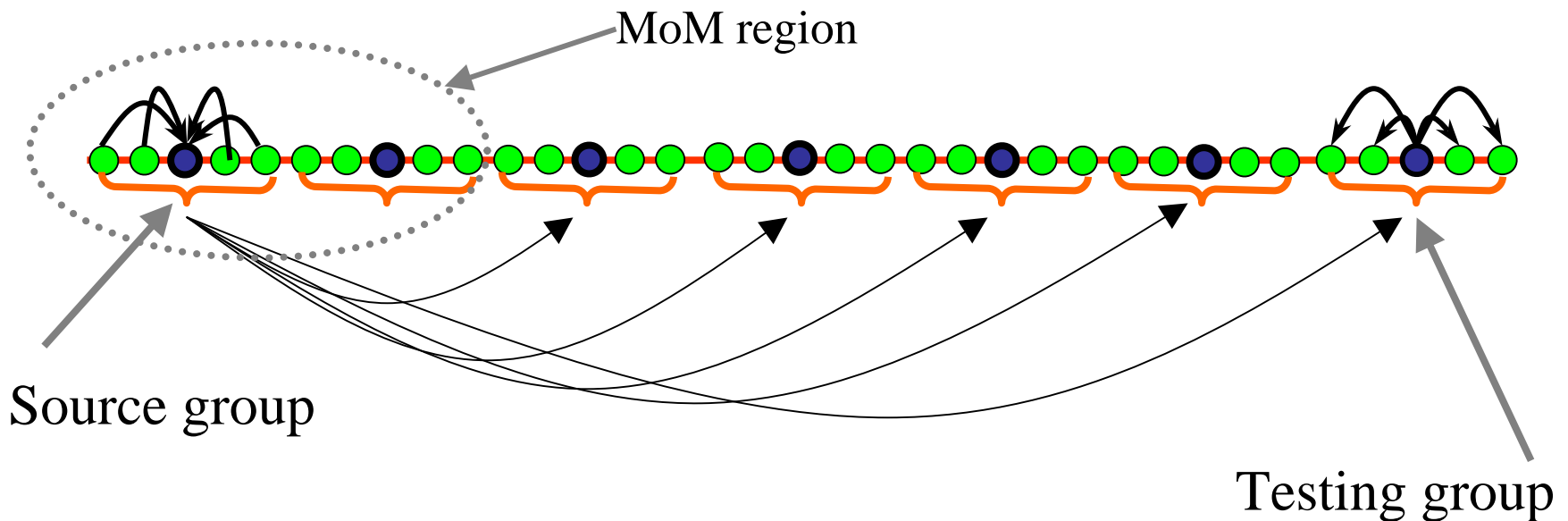


\*Every basis function interaction with all the testing function.  
Hence MoM has  $N^2$  interactions and  $N^2$  memory requirements.

# From MoM to Fast Multipole Method (FMM)

MoM: individual interaction between testing function and basis function.

FMM: group interaction between testing group and source group for far interactions (near interaction still use MoM scheme)



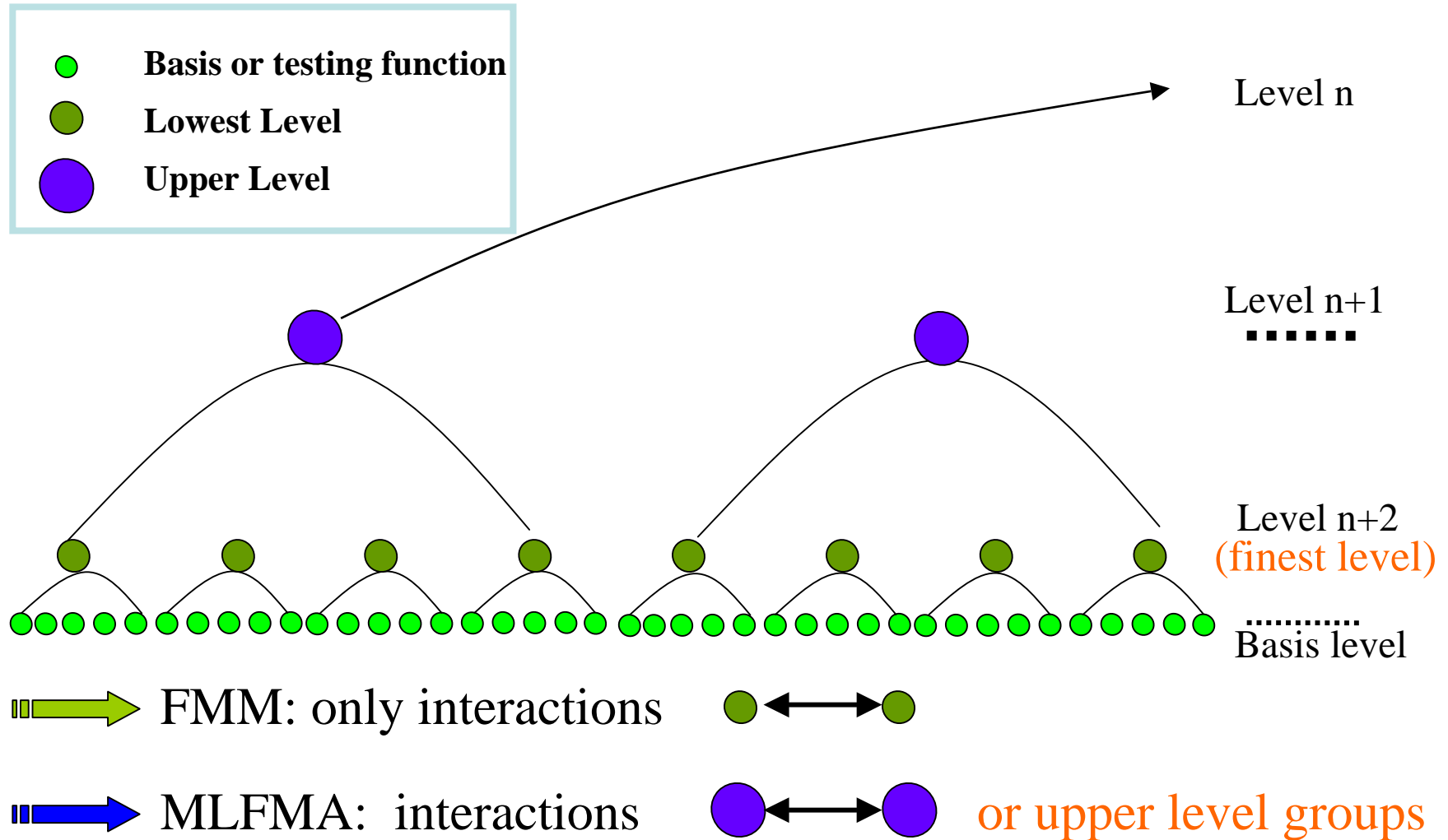
$$[\mathbf{Z}][\mathbf{J}] = \{ [\mathbf{Z}^{\text{near}}] + [\mathbf{Z}^{\text{far}}] \} [\mathbf{J}]$$

*diagonally dominant  
sparse matrix*

*handled by FMM on  
group-to-group basis*



# Multi-level Fast Multi-pole Algorithm (MLFMA)

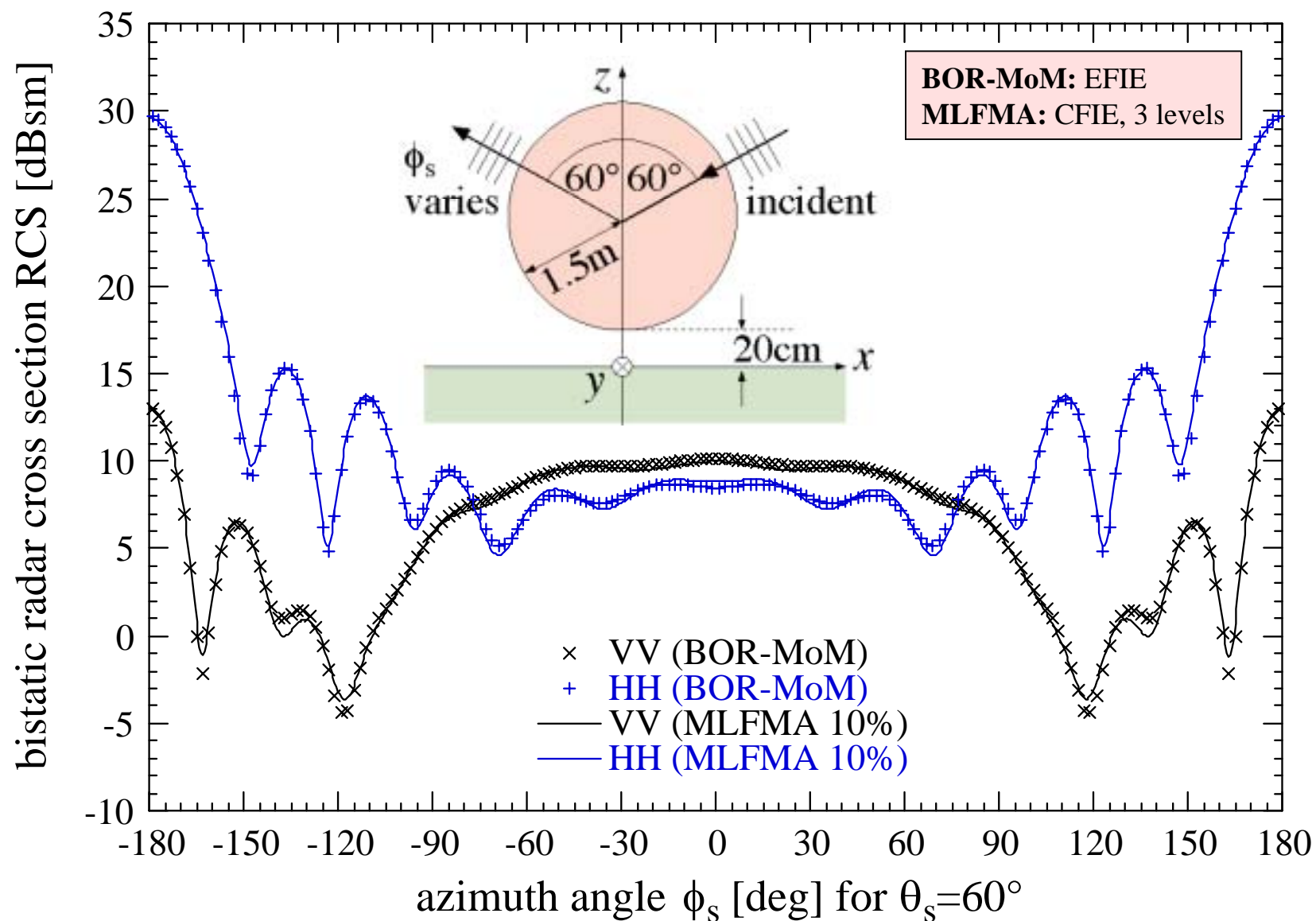


# RAM and CPU for MoM, FMM & MLFMA

	RAM	CPU (CG solver)
MoM	$O(N^2)$	$O(P \cdot N^2)$
FMM	$O(N^{1.5})$	$O(P \cdot N^{1.5})$
MLFMA	$O(N \log N)$	$O(P \cdot N \log N)$

# Bistatic RCS of Sphere ( $2a=3\lambda$ , $N=9966$ ) Above Soil

$f=300\text{MHz}$ ,  $a=1.5\text{m}$ ,  $\theta_i=60^\circ$ ,  $\phi_i=0^\circ$ ,  $\theta_s=60^\circ$ , Yuma soil: 10% water by weight



# T72 Tank/450MHz target $N=46,131$ unknowns

SGI runs:

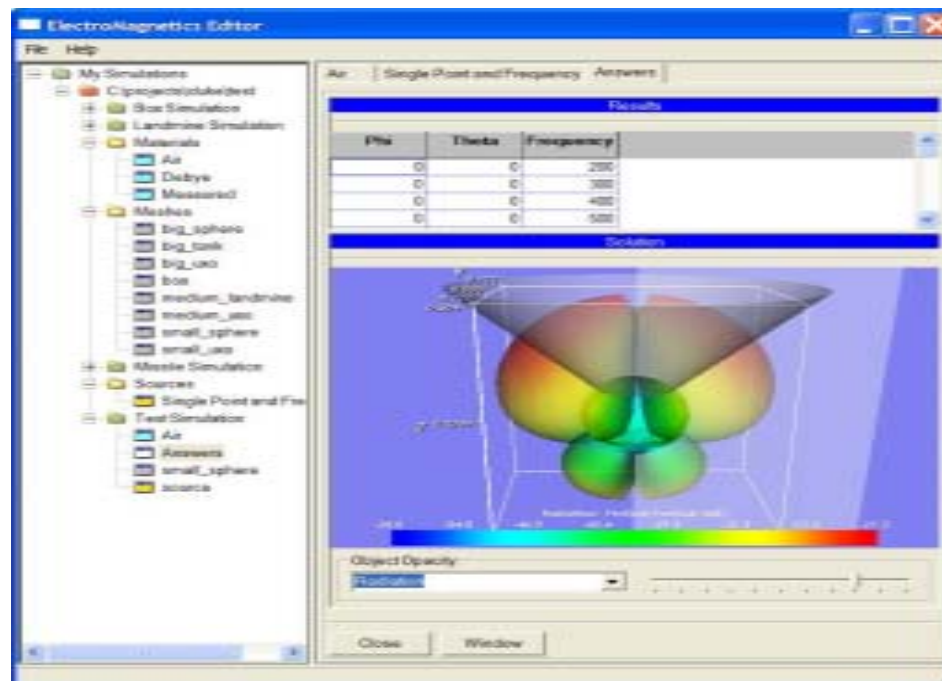
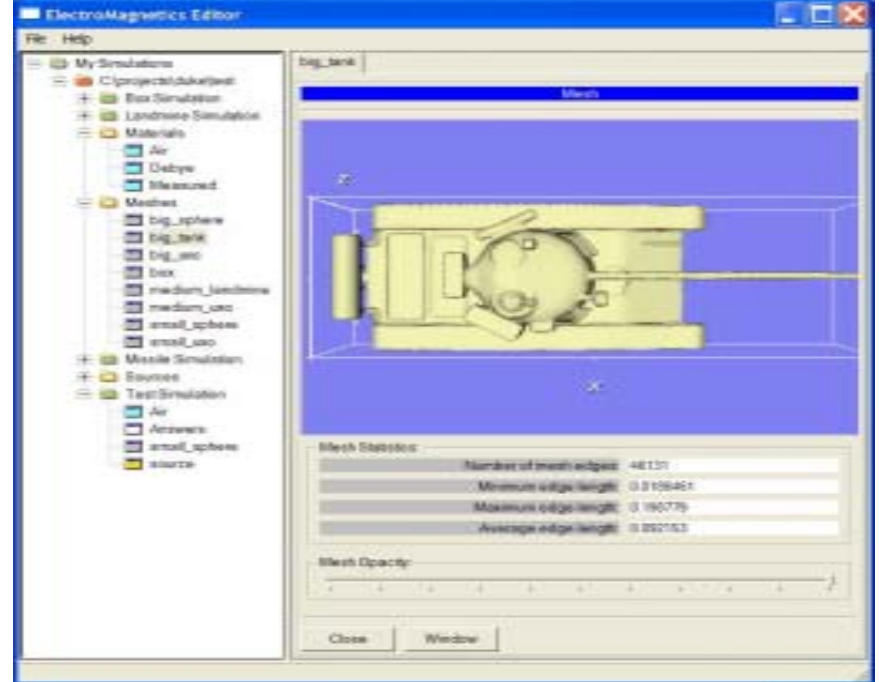
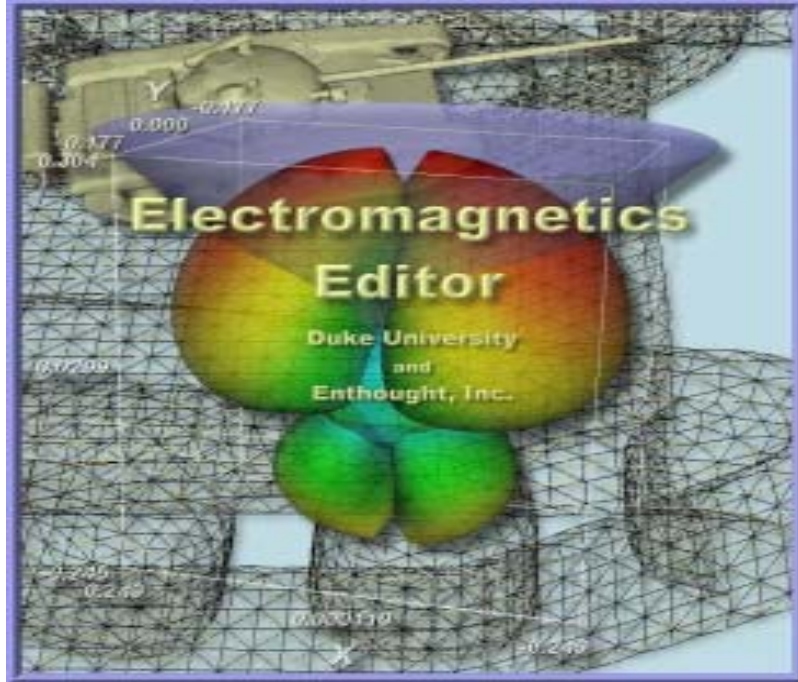
1 CPU	23999 sec	1.00 speed-up ( $= T_1/T_N$ )
2	18014	1.33
4	9065	2.65
8	3279	7.32
16	1947	12.32
32	1067	22.49
64	794	30.22

IBM runs:

4 CPUs	7241 sec	4.00 assumed speed-up
8	4651	6.23
16	2379	12.17
32	1581	18.32
64	1003	28.89

Beowulf cluster:

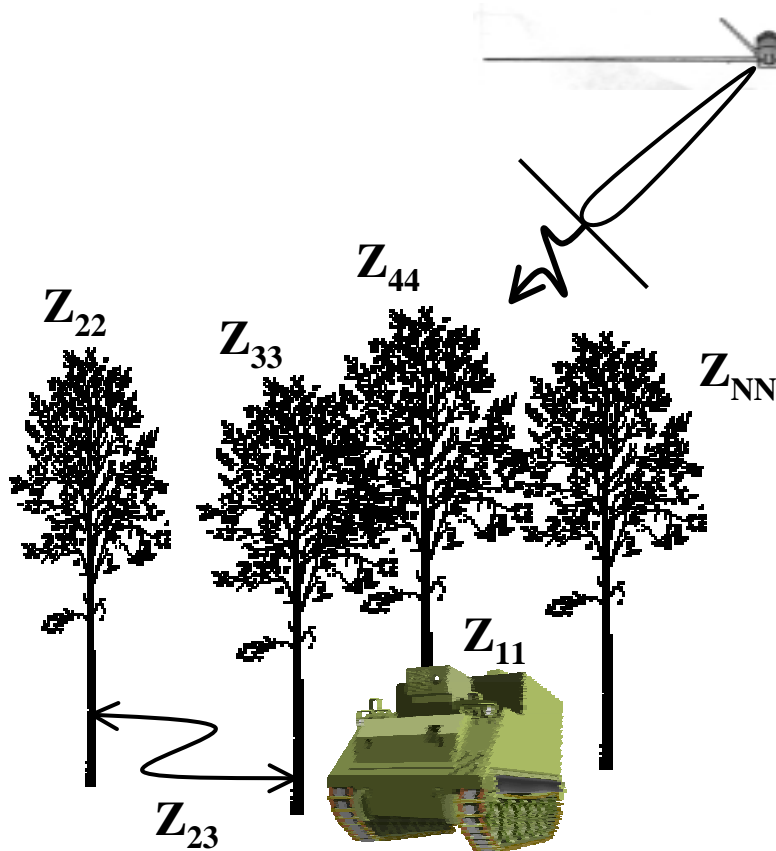
8 CPUs	4890
16	3802



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# Modeling Multiple Targets – Uncoupled



*MoM matrix grows as  $N^2$  with each additional target.*

*(Given size of target and wideband frequencies of interest, problem size grows beyond the capabilities of even supercomputers.)*

$$\begin{bmatrix} \mathbf{Z}_{11} & \mathbf{Z}_{12} & \mathbf{Z}_{13} & \Lambda \\ \mathbf{Z}_{21} & \mathbf{Z}_{22} & \mathbf{Z}_{23} & \Lambda \\ \mathbf{Z}_{31} & \mathbf{Z}_{32} & \mathbf{Z}_{33} & \Lambda \\ \mathbf{M} & \mathbf{M} & \mathbf{M} & \mathbf{O} \end{bmatrix} \begin{bmatrix} \mathbf{J}_1 \\ \mathbf{J}_2 \\ \mathbf{J}_3 \\ \mathbf{M} \end{bmatrix} = \begin{bmatrix} \mathbf{E}_1 \\ \mathbf{E}_2 \\ \mathbf{E}_3 \\ \mathbf{M} \end{bmatrix}$$



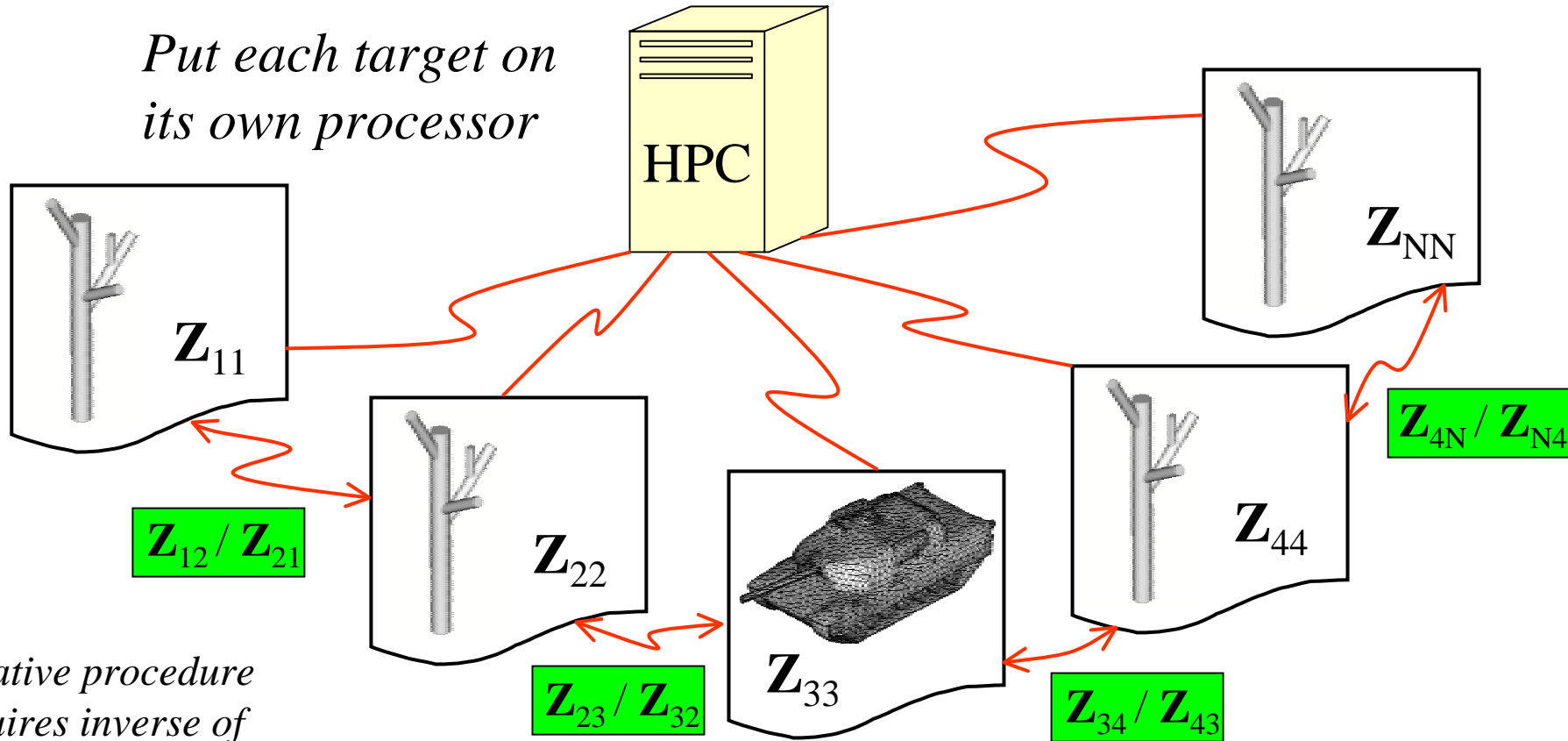
$$\begin{bmatrix} \mathbf{Z}_{11} & 0 & 0 & \Lambda \\ 0 & \mathbf{Z}_{22} & 0 & \Lambda \\ 0 & 0 & \mathbf{Z}_{33} & \Lambda \\ \mathbf{M} & \mathbf{M} & \mathbf{M} & \mathbf{O} \end{bmatrix} \begin{bmatrix} \mathbf{J}_1 \\ \mathbf{J}_2 \\ \mathbf{J}_3 \\ \mathbf{M} \end{bmatrix} = \begin{bmatrix} \mathbf{E}_1 \\ \mathbf{E}_2 \\ \mathbf{E}_3 \\ \mathbf{M} \end{bmatrix}$$



*For weak coupling ( $\mathbf{Z}_{ij} \approx 0, j \neq i$ ), an approximate simplified matrix can be written.*

# Modeling Multiple Targets – Coupled

*Put each target on its own processor*



*Iterative procedure requires inverse of diagonal matrices only*

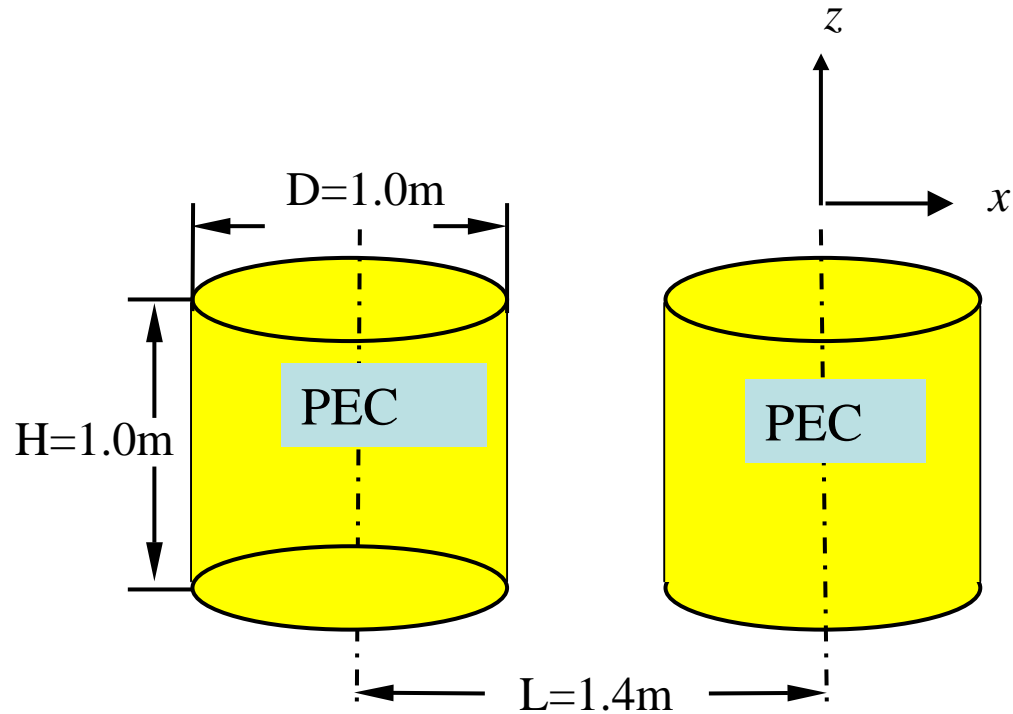
$$\begin{bmatrix} \mathbf{Z}_{11} & \mathbf{Z}_{12} & \mathbf{Z}_{13} & \Lambda \\ \mathbf{Z}_{21} & \mathbf{Z}_{22} & \mathbf{Z}_{23} & \Lambda \\ \mathbf{Z}_{31} & \mathbf{Z}_{32} & \mathbf{Z}_{33} & \Lambda \\ \mathbf{M} & \mathbf{M} & \mathbf{M} & \mathbf{O} \end{bmatrix} \begin{bmatrix} \mathbf{J}_1 \\ \mathbf{J}_2 \\ \mathbf{J}_3 \\ \mathbf{M} \end{bmatrix} = \begin{bmatrix} \mathbf{E}_1 \\ \mathbf{E}_2 \\ \mathbf{E}_3 \\ \mathbf{M} \end{bmatrix} \Rightarrow \begin{aligned} \mathbf{J}_1 &= \mathbf{Z}_{11}^{-1} \{ \mathbf{E}_1 - \mathbf{Z}_{12} \mathbf{J}_2 - \mathbf{Z}_{13} \mathbf{J}_3 - \Lambda \} \\ \mathbf{J}_2 &= \mathbf{Z}_{22}^{-1} \{ \mathbf{E}_2 - \mathbf{Z}_{21} \mathbf{J}_1 - \mathbf{Z}_{23} \mathbf{J}_3 - \Lambda \} \\ \mathbf{J}_3 &= \mathbf{Z}_{33}^{-1} \{ \mathbf{E}_3 - \mathbf{Z}_{31} \mathbf{J}_1 - \mathbf{Z}_{32} \mathbf{J}_2 - \Lambda \} \\ \mathbf{M} &= \mathbf{M} \end{aligned}$$

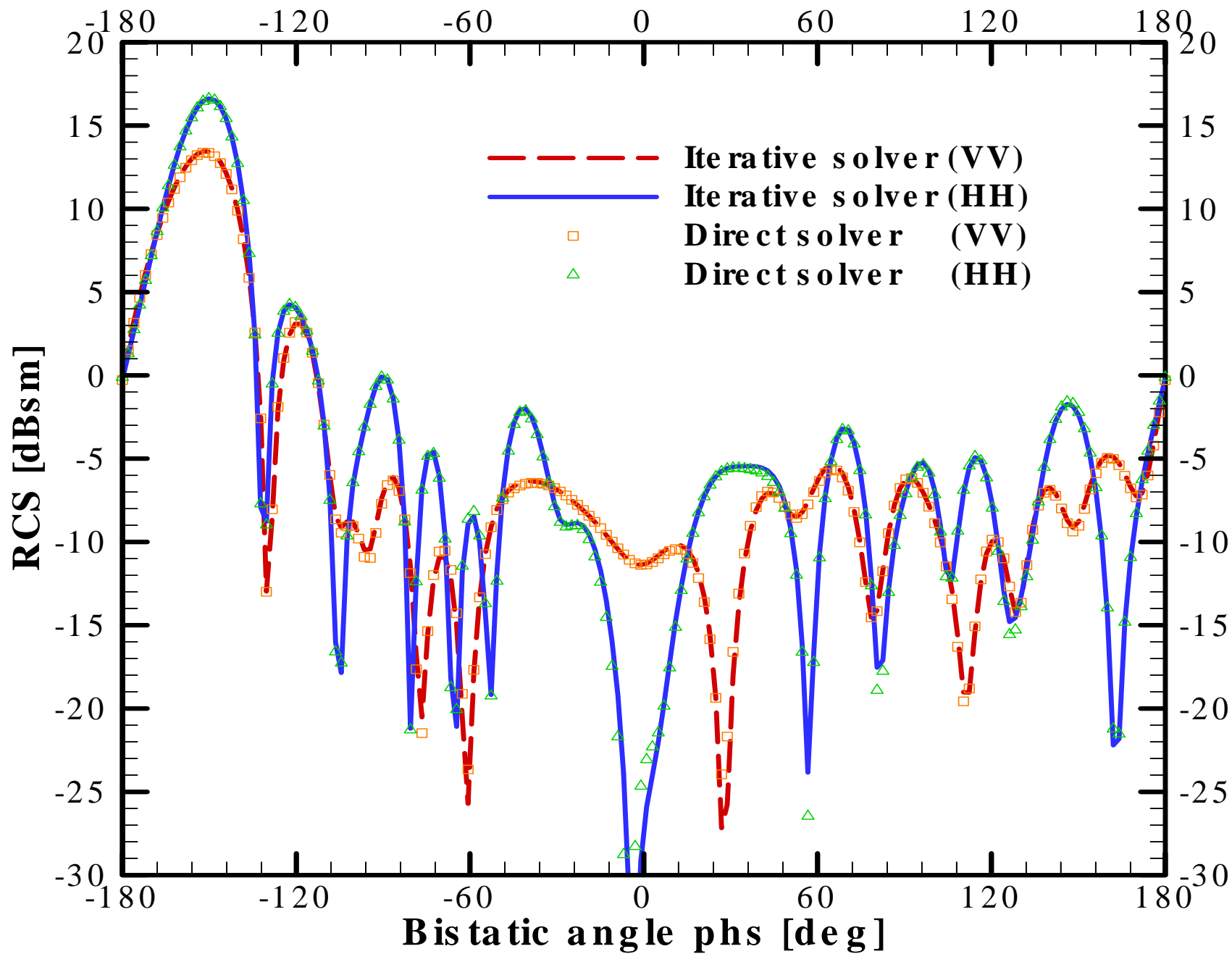


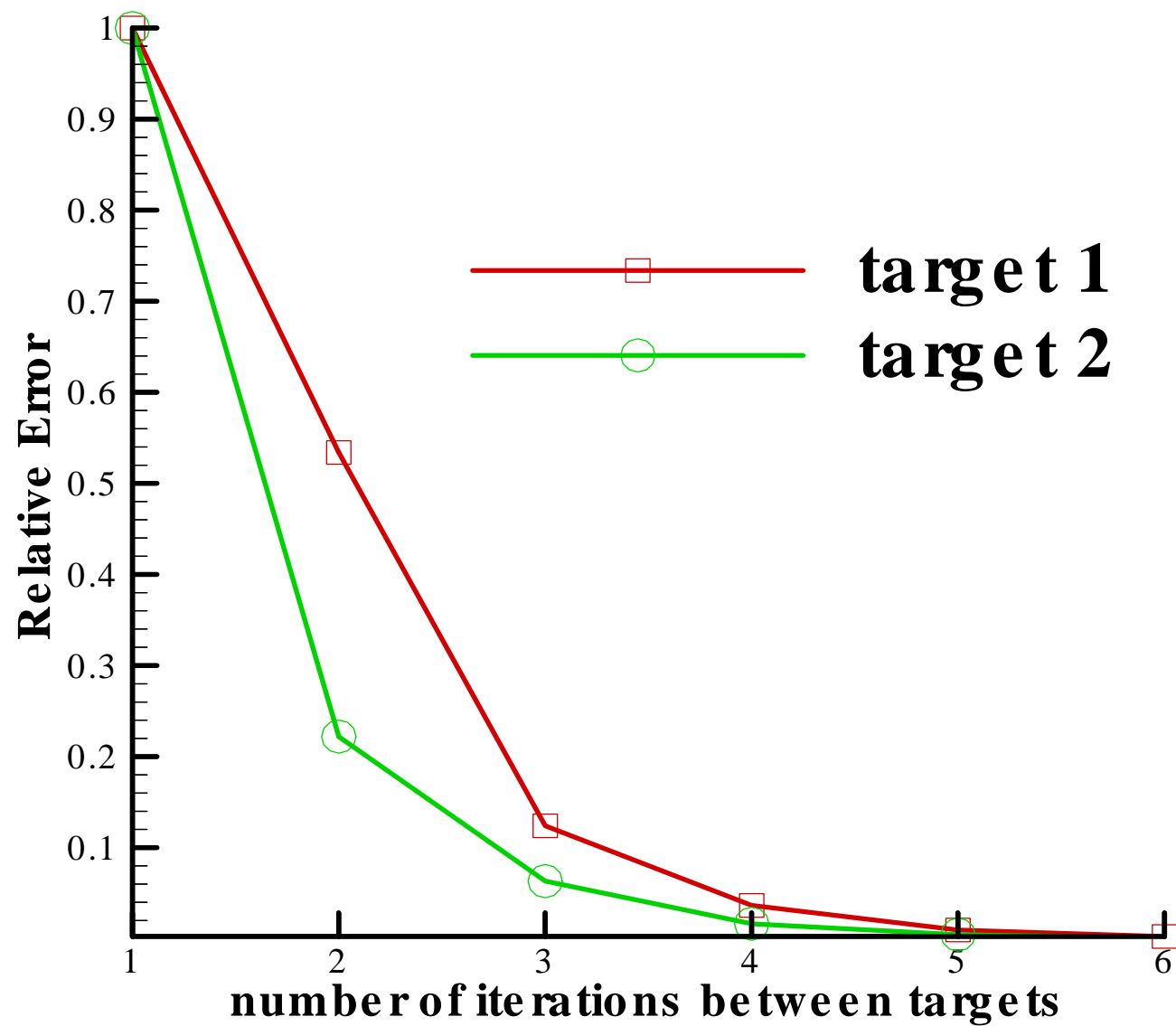
# Inter-Target Interactions

- For  $N_k$  basis functions on target  $k$ , and  $N_m$  on target  $m$ , direct computation of inter-target scattering is  $O(N_k N_m)$
- Have employed the FMM to efficiently account for inter-target scattering
- For targets  $k$  and  $m$ , we utilize the largest FMM box (cluster) sizes that allows *all* interactions to be handled via “far” terms
- Box sizes are target dependent and inter-target-distance dependent
- For targets separated further than nominal target sizes, each target placed within single FMM box
- Inter-target-scattering propagator communicated efficiently via MPI (each target on a separate computer node)

# Freespace Targets







# Coupled Model Over Half-Space

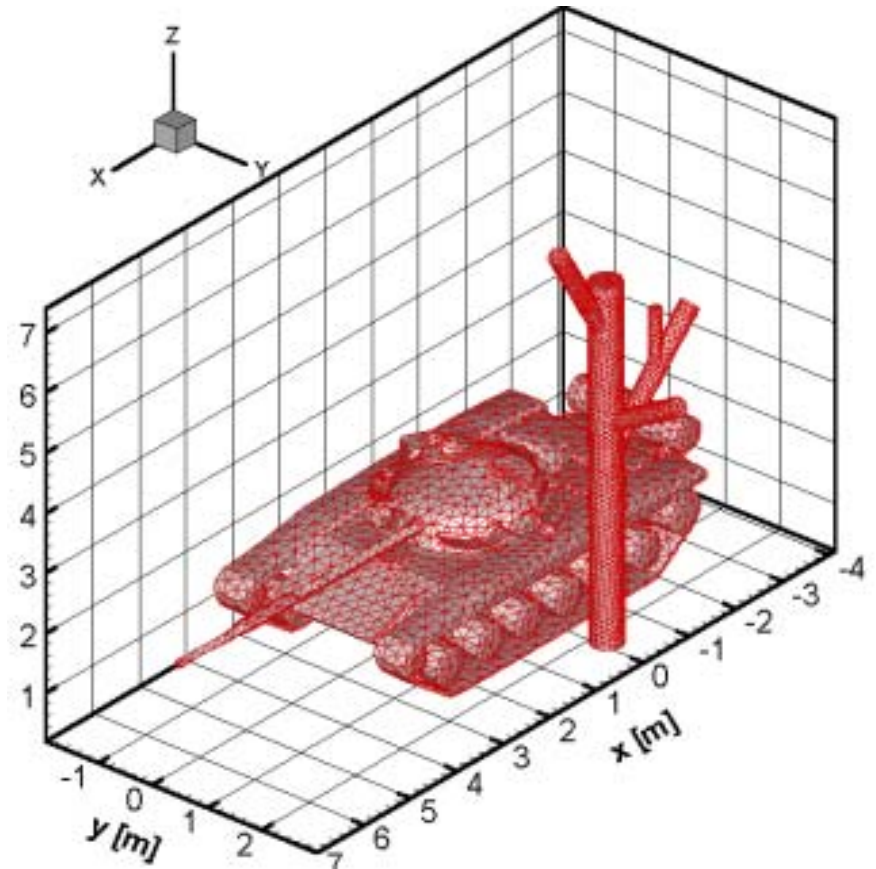
Tank, tree, and ground composite model:

Coupled – all interactions accounted for.

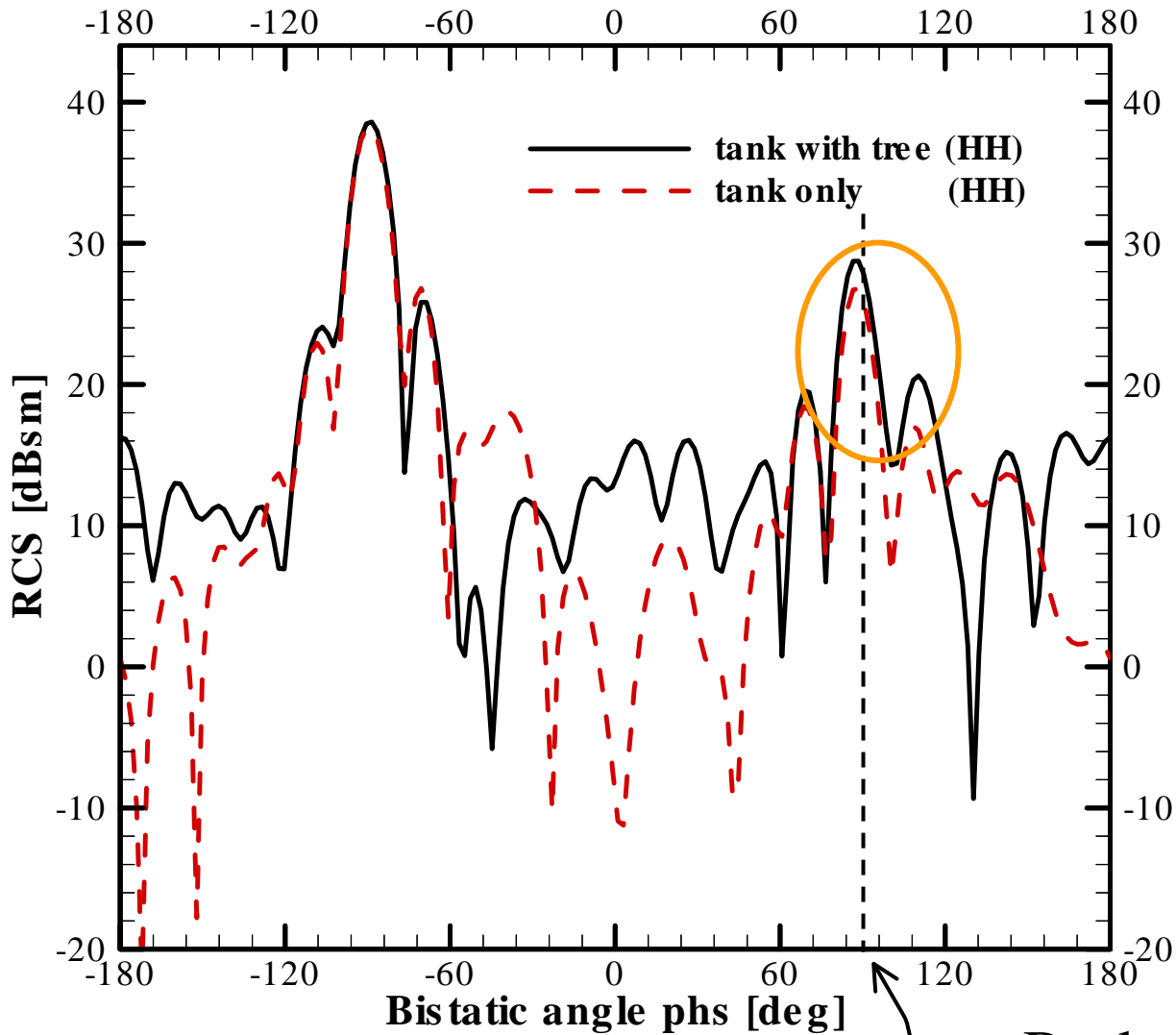
$\theta=45$  degrees

$\phi=90$  degrees (broadside)

frequency=300 MHz



# Bistatic RCS of Tank vs. Tank and Tree: HH



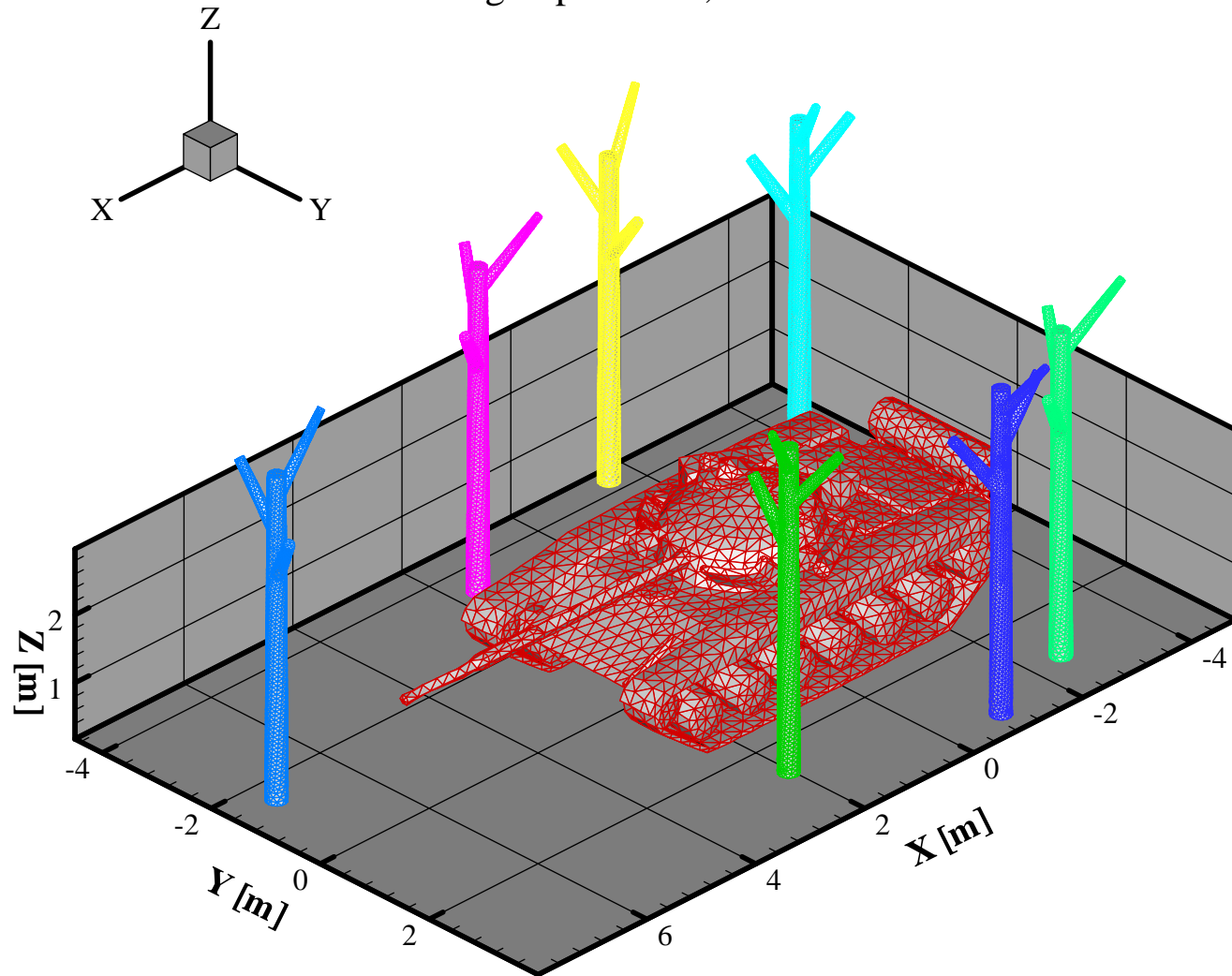
*Monostatic RCS changes little as a result of tree shadowing.*

Backscatter angle

# Tank with 7 trees in half space

Diameter of the tree trunk: 30cm, Height: 5m

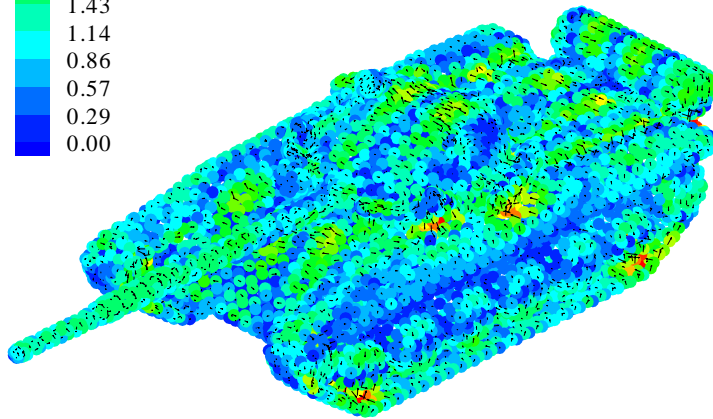
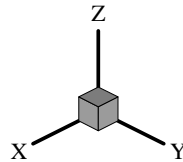
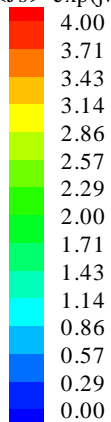
Incident angle:  $\phi = 90^\circ$ ,  $\theta = 45^\circ$



# Current Distribution – Vpol

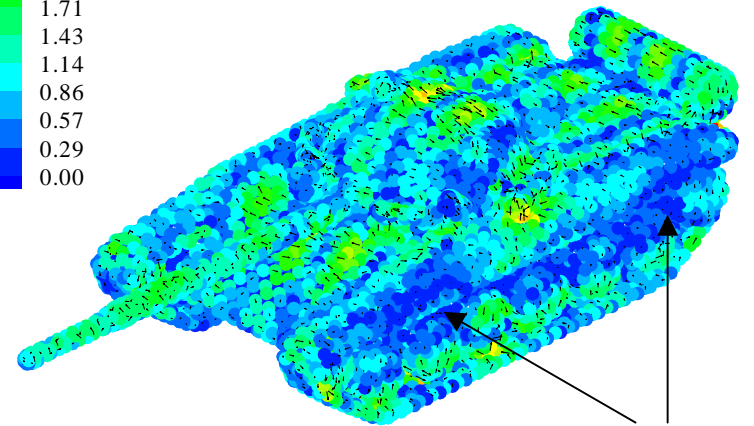
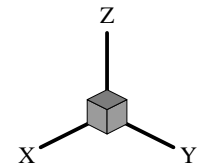
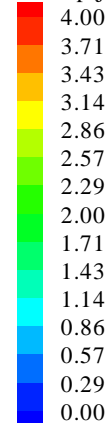
Isolated tank

$|\text{Re}(\langle J_s \rangle * \exp(j\omega t)/H_0)|$  (v)



Tank with all trees present

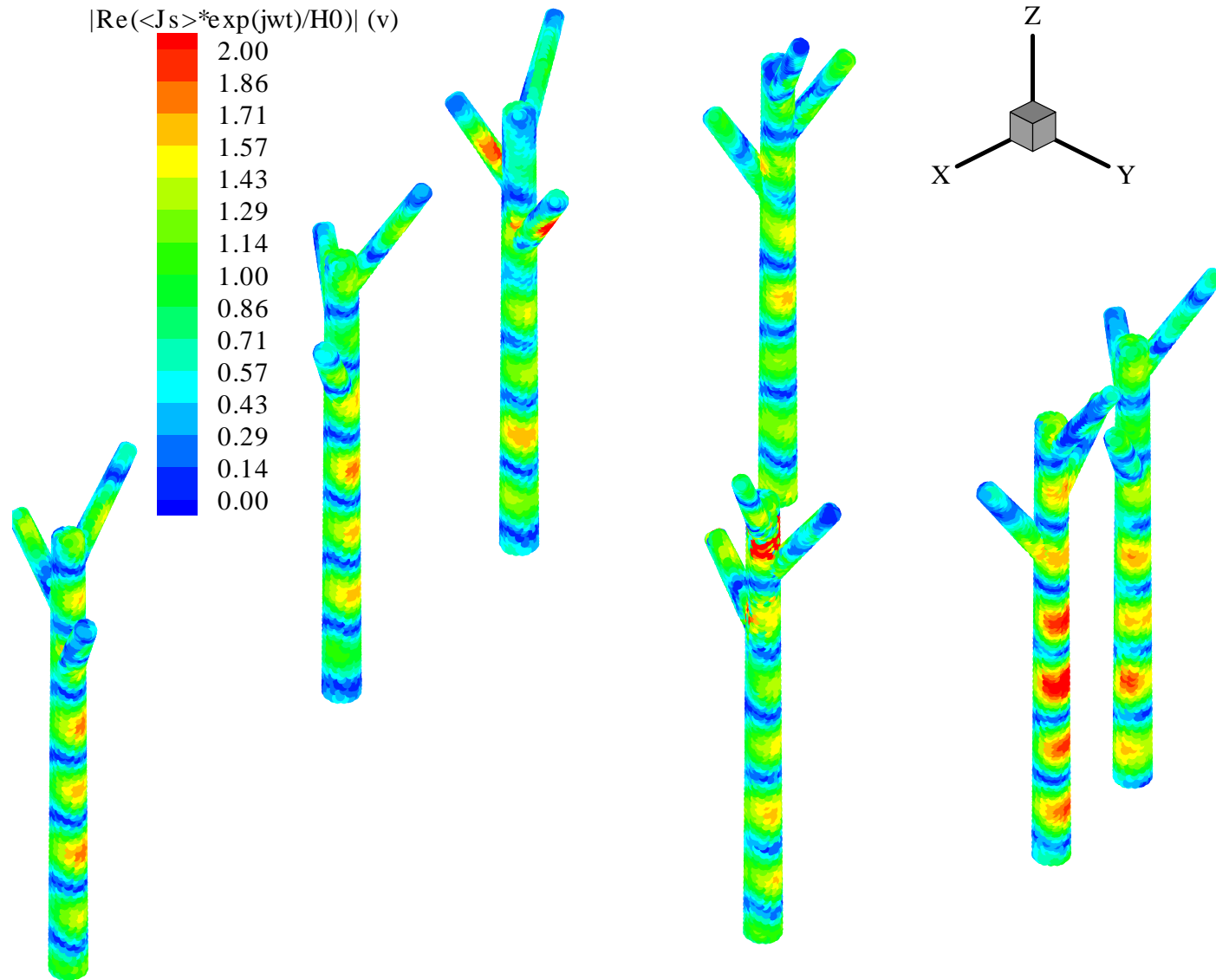
$s * \exp(j\omega t)/H_0)|$  (v)



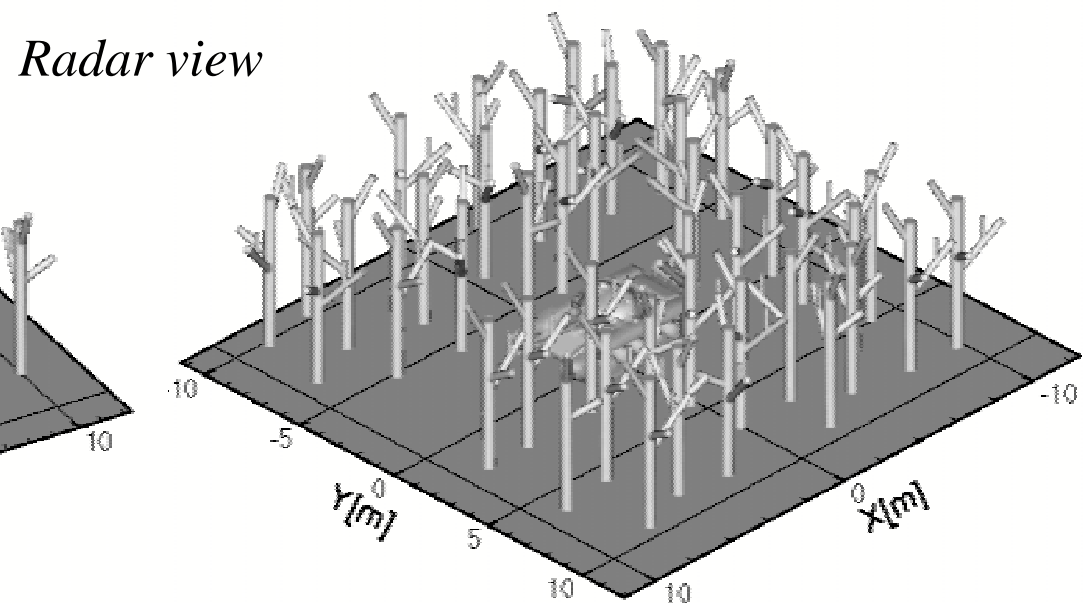
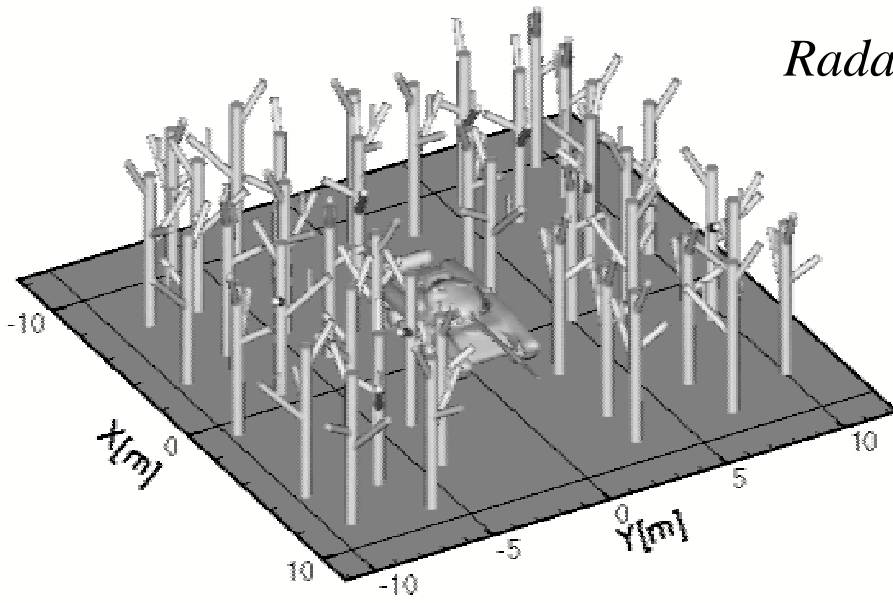
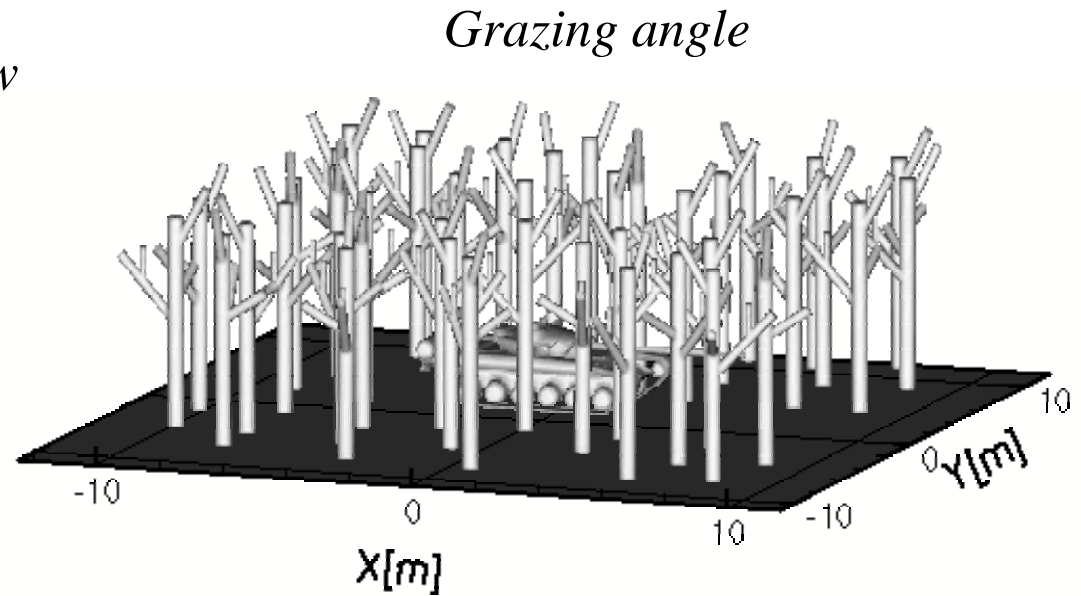
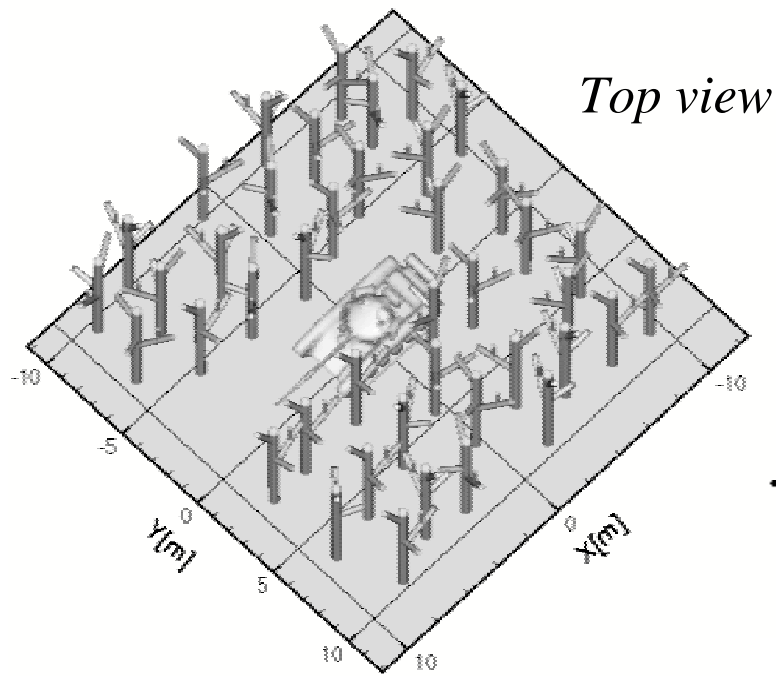
*shadows*



# Current distribution on trees - Vpol



# Ultimately Want to get Here – SAR Forest Model



# Summary

- Scalable MLFMA developed and tested for general PEC/dielectric targets above/below a half space
- Scalable software now capable of efficiently analyzing scattering from and propagation through an arbitrary number of dielectric/PEC targets in the presence of a half space
- Code can be modified to handle communications problem (e.g., antenna mounted on vehicle)
- Beta version of CEA-9 to be released this August
  - can visit the web site: <http://webtech.ee.duke.edu/cgi-bin/chssi/news>